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- Early computer programming was difficult
 - Not only because interacting with the computer was difficult
 - Data was entered by setting switches, using punched tapes or cards, electromagnetic tapes, etc
 - But also interaction was at the machine level
 - Earliest instructions were in binary

- Assembler were invented to translate human readable instructions into machine language
- Only later were "higher level programming languages" developed such as Fortran (for FORmula TRANslator) and Cobol (COmmon Business Language)

- Some tasks were also repetitive
 - Such as calculating the sine of a number
 - The necessity to calculate sine gave rise to the first procedure
 - The procedure expect its input at a certain location
 - It writes it output at another certain location
 - It consists of a block of lines of code
 - Procedure calling works like this:
 - The caller loads the input locations with the data
 - It also stores the address of the next instruction at a well-known location, the *return* address
 - Program control jumps to the beginning of the procedure
 - The procedure executes and loads its results in the output locations
 - The procedure then jumps to the *return address*
 - The caller finds the result at a certain location

- Besides the capability to re-use code, sub-procedures were also an important tool to break a complicated task into smaller pieces
- This is called modularization
- It's been a main-stay in software engineering ever since

- Python almost completely uses the abstraction of a function
- A function is called from the caller, given none or a number of *arguments* (aka parameters)
- The function returns to the caller
 - Giving a return value (a *fruitful* function)
 - Or just returning

- Calling fruitless functions
 - We already have used a fruitless function, namely print
 - print is special, it can have any number of arguments
 - Example: print("The value is", 3.145)
 - Two arguments
 - String "The value is"
 - Floating point 3.145

- We can use built-in fruitful functions
 - abs returns the absolute value

>>> abs(-4) 4

- We can import the module math in order to have access to many mathematical functions
 - A complete list is in the Python Docs.
 - Here we just print out the values of some functions.

```
mathmodule.py - /Users/thomasschwarz/Documents/My website/Classes/Module...
import math
x = 2.56
print(x, math.sin(x), math.exp(x), math.log(x, 2), math.log(x, 10), math.log(x))
```

Creating functions

def function_name (parameter_list) :

Statement Block

- Uses key word def
- Followed by the name of the function (usually lower-letter)
- In parentheses, a list of arguments (aka parameters) separated by comma
- Followed by colon

- Example for a fruitless function
 - Function that prints out *n* asterisks, then a blank line, then *n* asterisks

```
def asterisks(n):
    print(n*"*")
    print()
    print(n*"*")
```

- There is a single argument, *n*
 - Note that *n* does not have a specified type.
 - Since in the body of the function, we multiply with *n*, it better be an integer.

- Example for a fruitless function
 - Function that prints out *n* asterisks, then a blank line, then *n* asterisks

```
def asterisks(n):
    print(n*"*")
    print()
    print(n*"*")
```

- Three statements follow in the function block.
- The function execution finishes, when we fall out of the block
- If we want to be explicit, we can add a final line to the function block with the single statement return

- Example for a fruitful function
 - A function that given x and y, calculates the expression

$$\frac{|x-y|}{x^2+y^2}$$

 The function needs two arguments and needs to return a value

$$x, y \to \frac{|x - y|}{x^2 + y^2}$$

def fun(x, y):
 enumerator = abs(x-y)
 denominator = x*x+y*y
 return enumerator/denominator

- There are now two arguments, separated by a comma
- The body of the function calculates the result
- The result is returned with the return-statement.
- An exception will be thrown if we call the function with values 0 and 0 since we then divide by zero in the calculation of the function.

- We can have more than one return statement
 - An implementation of the maximum of two numbers function

def my_max(x,y):
 if x<y:
 return y
 return x</pre>

 I do not need to put the last line in an else, since if x<y, then I already jumped out of the execution of the function body.