

$$\geq \sqrt{n} \cdot D \sqrt{n \log(\log(\sqrt{n}))} + n$$