

$$v_{i+1}.\text{dist} = v_i.\text{dist} + 1 \leq v_1.\text{dist} + 1$$