

$$v_n.\text{dist} \leq v.\text{dist} + 1 \leq v_{n+1}.\text{dist}$$