

$$v_n.\text{dist} \leq v_1.\text{dist} + 1 \leq v_2.\text{dist} + 1$$