

Module 9: Lists

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Lists

- Python is a high-level programming language with built-in sophisticated data structures
- The simplest of these data structures is the list.
- A list is just an ordered collection of other objects
 - The type of the objects is not restricted
- Let's start unpacking this a bit.

Lists

- We create a list by using the square brackets.
 - `alist = [1, 3.5, "hello"]`
 - A list with three elements of three different types
 - `blist = [1, 3.5, "hello", 1]`
 - A list with four elements, where one element is repeated
 - `clist = [1, "hello", 3.5]`
 - A different list than `alist`, but with the same elements
 - The order is different

Lists

- Accessing elements in a list
 - We access elements in a list by using the square brackets and an index
 - Indices start at 0
- Example:
 - `lista = ['a', 'b', 'c', 'd']`
 - `lista[0]` is 'a'
 - `lista[1]` is 'b'
 - `lista[2]` is 'c'

Lists

- Python uses negative numbers in order to count from the back of the list
 - `lista = ['a', 'b', 'c', 'd']`
 - `lista[-1]` is the last object, namely the character 'd'
 - `lista[-2]` is the second-last object, namely the character 'c'
 - `lista[-4]` is the first object, namely the character 'a'

Manipulating Lists

- We manipulate lists by calling list methods
 - You should read up on lists in the Python documentations
 - <https://docs.python.org/3/tutorial/datastructures.html>
- The length (number of objects in a list) is obtained by the len function.

```
>>> lista = [1, 2, 3]
>>> len(lista)
3
```

Manipulating Lists

- We add to a list by using the append method

- Example:

```
>>> lista = [1, 2, 3]
>>> lista.append(5)
>>> lista.append([1,2])
>>> print(lista)
[1, 2, 3, 5, [1, 2]]
```

- The resulting list `lista` has five elements, the last one being a list by itself.
- The append method always adds an element at the end.

Manipulating Lists

- The opposite of *append* is *pop*.
 - Whereas *append* returns the special object *None*, *pop* removes the last element in the list and returns it.
- Example

```
>>> lista = [1,2,3]
>>> lista.pop()
3
>>> print(lista)
[1, 2]
```


Manipulating Lists

- We can also combine two lists with extend.
 - The method parameter is a list that is added to the first list.

```
>>> list1 = [1, 2, 3]
>>> list2 = [4, 5]
>>> list1.extend(list2)
>>> list1
[1, 2, 3, 4, 5]
```

- This is different than appending.

```
>>> list1 = [1, 2, 3]
>>> list2 = [4, 5]
>>> list1.append(list2)
>>> print(list1)
[1, 2, 3, [4, 5]]
```

- The resulting list has four elements, with the last one being a list

Manipulating Lists

- To remove items from a list, we can use
 - remove
 - del
- The remove method removes the first element from the list that matches a parameter
 - It does not remove all elements
 - Example:

```
>>> lista = [1, 2, 3, 4, 5, 1, 1, 2, 2, 2, 3]
>>> lista.remove(1)
>>> lista
|[2, 3, 4, 5, 1, 1, 2, 2, 2, 3]
```

Manipulating Lists

- del operator:
 - A generic operator
 - In order to remove an item from a list, you specify a list and an index
 - Example: Remove the third element (“c”) from a list

```
>>> lista = ["a", "b", "c", "d", "e"]
>>> del lista[2]
>>> lista
['a', 'b', 'd', 'e']
```

Manipulating Lists: A Standard Pattern

- A pattern for list modification
 - Often, we need to process a list
 - A standard pattern:
 - Create an empty result list
 - Walk through the processed list
 - Add elements to the result list

Manipulating Lists: A Standard Pattern

- Example:
 - Filtering:
 - Retain all elements in a list that are even numbers

```
def even(lista):  
    result = []  
    for ele in lista:  
        if ele%2==0:  
            result.append(ele)  
    return result
```

Create the result as an empty list

```
>>> even([1,2,3,6,7,98,12,324,43,56,15,37,45])  
[2, 6, 98, 12, 324, 56]
```

Manipulating Lists: A Standard Pattern

- Example:
 - Filtering:
 - Retain all elements in a list that are even numbers

```
def even(lista):  
    result = []  
    for ele in lista:  
        if ele%2==0:  
            result.append(ele)  
    return result
```

Walk through the list

```
>>> even([1,2,3,6,7,98,12,324,43,56,15,37,45])  
[2, 6, 98, 12, 324, 56]
```

Manipulating Lists: A Standard Pattern

- Example:
 - Filtering:
 - Retain all elements in a list that are even numbers

```
def even(lista):  
    result = []  
    for ele in lista:  
        if ele%2==0:  
            result.append(ele)  
    return result
```

Filter on condition

```
>>> even([1,2,3,6,7,98,12,324,43,56,15,37,45])  
[2, 6, 98, 12, 324, 56]
```

Manipulating Lists: A Standard Pattern

- Example:
 - Filtering:
 - Retain all elements in a list that are even numbers

```
def even(lista):  
    result = []  
    for ele in lista:  
        if ele%2==0:  
            result.append(ele)  
    return result
```

Append to the result

```
>>> even([1,2,3,6,7,98,12,324,43,56,15,37,45])  
[2, 6, 98, 12, 324, 56]
```


Manipulating Lists: A Standard Pattern

- Example:
 - Filtering:
 - Retain all elements in a list that are even numbers

```
def even(lista):  
    result = []  
    for ele in lista:  
        if ele%2==0:  
            result.append(ele)  
    return result
```

Return the result

```
>>> even([1,2,3,6,7,98,12,324,43,56,15,37,45])  
[2, 6, 98, 12, 324, 56]
```

Manipulating Lists: A Standard Pattern

- Example:
 - Map — transforming all elements in a list
 - Given a list of numbers, round them to the nearest digit after the decimal point

Manipulating Lists: A Standard Pattern

- Example:

```
def rounding(lista):  
    result = []  
    for ele in lista:  
        result.append(round(ele, 1))  
    return result
```

Create an empty list

```
>>> rounding([.113241, 123.45, 1342.68, 12, 123.456, 908.17, -89.1])  
[0.1, 123.5, 1342.7, 12, 123.5, 908.2, -89.1]
```

Manipulating Lists: A Standard Pattern

- Example:

```
def rounding(lista):  
    result = []  
    for ele in lista:  
        result.append(round(ele, 1))  
    return result
```

Walk through the list

```
>>> rounding([.113241, 123.45, 1342.68, 12, 123.456, 908.17, -89.1])  
[0.1, 123.5, 1342.7, 12, 123.5, 908.2, -89.1]
```

Manipulating Lists: A Standard Pattern

- Example:

```
def rounding(lista):  
    result = []  
    for ele in lista:  
        result.append(round(ele, 1))  
    return result
```

Apply the function to the list
element

```
>>> rounding([.113241, 123.45, 1342.68, 12, 123.456, 908.17, -89.1])  
[0.1, 123.5, 1342.7, 12, 123.5, 908.2, -89.1]
```

Manipulating Lists: A Standard Pattern

- Example:

```
def rounding(lista):  
    result = []  
    for ele in lista:  
        result.append(round(ele, 1))  
    return result
```

Append to the result

```
>>> rounding([.113241, 123.45, 1342.68, 12, 123.456, 908.17, -89.1])  
[0.1, 123.5, 1342.7, 12, 123.5, 908.2, -89.1]
```

Manipulating Lists: A Standard Pattern

- Example:

```
def rounding(lista):  
    result = []  
    for ele in lista:  
        result.append(round(ele,1))  
    return result
```

Return the result

```
>>> rounding([.113241, 123.45, 1342.68, 12, 123.456, 908.17, -89.1])  
[0.1, 123.5, 1342.7, 12, 123.5, 908.2, -89.1]
```

Manipulating Lists: A Standard Pattern

- We can generate this example to all functions of list elements

```
def apply(function, lista):  
    result = []  
    for ele in lista:  
        result.append(function(ele))  
    return result
```

- This pattern is so important that Python 3 has a more elegant way of doing it. It is called list comprehension
 - The apply function was part of Python 2, depreciated in Python 2.3 and abolished in Python 3.5

Lists are objects

- Lists are objects
 - Objects have methods
 - Methods are functions that are called with an object as a parameter, but that are specific to the object
 - We write them as
object . method (additional, optional parameters)
 - In fact, method is a function and object is the first and sometimes only parameter

Methods vs. Function

- There are two built-in ways to sort a list in Python:
 - The sorted function
 - The sort method for lists
- They are called differently because one is a method and one a function
 - sorted returns a sorted list
 - *.sort() does not return anything, but the list is sorted.

```
>>> lista = ['c', 'b', 'a', 'd']
>>> lista.sort()
>>> lista
['a', 'b', 'c', 'd']
>>> lista = ['c', 'b', 'a', 'd']
>>> sorted(lista)
['a', 'b', 'c', 'd']
```

Manipulating Lists

- Here is an overview of the most important list methods:

Method	Effect
<code>append()</code>	adds an element to the end of the list
<code>clear()</code>	removes all elements from a list
<code>copy()</code>	returns a copy of the list
<code>count()</code>	returns the number of elements in the list
<code>extend()</code>	adds the elements in the parameter to the list
<code>index()</code>	returns the index of the first occurrence of the parameter
<code>insert()</code>	inserts an element at the specified location
<code>pop()</code>	removes an element at the specified location or if left empty, removes the last element
<code>remove()</code>	removes the first element with that value
<code>reverse()</code>	reverses the order of the list
<code>sort()</code>	sorts the list

Range is not a list

- A range belongs to a data structure (called iterators) that are related to lists
 - In an iterator, you can always produce the next element
 - To make a list, just use the list keyword:

```
lista = list(range(2, 1000))
```

Lists and for loops

- The for-loop in Python iterates through a list (or more generally an iterator)
 - `for x in lista:`
 - `x` takes on all values in `lista`

Checking membership

- In Python, membership in a list is checked with the `in` keyword
 - There is a more appealing, alternative form of negation
- Examples:
 - `if element in lista:`
 - `if element not in lista:`
 - Use this one instead of the negation around the statement
 - `if not element in lista:`

Sieve of Eratosthenes

- To calculate a list of all primes, we could:
 - Check all numbers in $[2, 3, 4, \dots, n]$ that have no divisors
 - Which is tedious and does not scale to large n
 - Eliminate all multiples
 - This is the idea behind the famous Sieve of Eratosthenes

Sieve of Eratosthenes

- We start out with a list of all numbers between 2 and 1000
 - [2, 3, 4, 5, 6, 7, ... , 999, 1000]
- The smallest number in the list is a prime, this would be 2
 - We can eliminate all true multiples of 2, that is, we remove 4, 6, 8, 10, ... , 1000 from the list
 - This gives us
 - [2, 3, 5, 7, 9, 11, 13, ..., 997, 999]
- The next smallest number has also to be a prime

Sieve of Eratosthenes

- [2, 3, 5, 7, 9, 11, 13, 15, 17, ..., 997, 999]
- Therefore, 3, is a prime.
- For the next step, we eliminate all multiples of three that are left
 - [2, 3, 5, 7, 11, 13, 17, 19, 23, 25, 29, ... ,995, 997]
- We remove all multiples of 5 that remain in the list: 25, 35, 55, ...
 - [2, 3, 5, 7, 11, 13, 17, 19, 23, 29, ... ,991, 997]
- And so we continue, until we can no longer eliminate multiples

Sieve of Eratosthenes

- We implement this in Python
 - We first define a function that removes multiples of an element from a list (of numbers)
 - We need one parameter `limit` to tell us when we should stop

```
def remove_multiples(element, lista, limit):  
    multiplier = 2  
    while multiplier*element <= limit:  
        if multiplier*element in lista:  
            lista.remove(multiplier*element)  
        multiplier += 1
```

Sieve of Eratosthenes

- We can now implement the sieve
 - We initialize a list to the first 1000 elements
 - We maintain an index to tell us to which of the elements we already processed

```
def eratosthenes():  
    lista = list(range(2, 1000))  
    index = 0
```

Sieve of Eratosthenes

- We stop when the index is about to fall out of the current size of the list
- Don't forget to increase the index

```
def eratosthenes():  
    lista = list(range(2, 1000))  
    index = 0  
    while index < len(lista):  
        #Do the work here  
        index += 1
```

Sieve of Eratosthenes

- The work to do for each index is to remove the multiples of the current element

```
def eratosthenes():  
    lista = list(range(2, 1000))  
    index = 0  
    while index < len(lista):  
        element = lista[index]  
        remove_multiples(element, lista, limit)  
        index += 1
```

Sieve of Erathosthenes

- And here is the result, all primes until 1000

```
[2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 49, 53, 59, 61, 67, 71, 73,
77, 79, 83, 89, 91, 97, 101, 103, 107, 109, 113, 119, 121, 127, 131, 133, 137, 139,
143, 149, 151, 157, 161, 163, 167, 169, 173, 179, 181, 187, 191, 193, 197, 199, 203,
209, 211, 217, 221, 223, 227, 229, 233, 239, 241, 247, 251, 253, 257, 259, 263, 269,
271, 277, 281, 283, 287, 289, 293, 299, 301, 307, 311, 313, 317, 319, 323, 329, 331,
337, 341, 343, 347, 349, 353, 359, 361, 367, 371, 373, 377, 379, 383, 389, 391, 397,
401, 403, 407, 409, 413, 419, 421, 427, 431, 433, 437, 439, 443, 449, 451, 457, 461,
463, 467, 469, 473, 479, 481, 487, 491, 493, 497, 499, 503, 509, 511, 517, 521, 523,
527, 529, 533, 539, 541, 547, 551, 553, 557, 559, 563, 569, 571, 577, 581, 583, 587,
589, 593, 599, 601, 607, 611, 613, 617, 619, 623, 629, 631, 637, 641, 643, 647, 649,
653, 659, 661, 667, 671, 673, 677, 679, 683, 689, 691, 697, 701, 703, 707, 709, 713,
719, 721, 727, 731, 733, 737, 739, 743, 749, 751, 757, 761, 763, 767, 769, 773, 779,
781, 787, 791, 793, 797, 799, 803, 809, 811, 817, 821, 823, 827, 829, 833, 839, 841,
847, 851, 853, 857, 859, 863, 869, 871, 877, 881, 883, 887, 889, 893, 899, 901, 907,
911, 913, 917, 919, 923, 929, 931, 937, 941, 943, 947, 949, 953, 959, 961, 967, 971,
973, 977, 979, 983, 989, 991, 997]
```

Sieve of Eratosthenes

- This implementation can be improved in a number of ways
 - For example, we do not need to remove all multiples because we know that they have been removed
 - For example, if we are processing 13, then we do not need to check for $2 \cdot 13$, $3 \cdot 13$, $4 \cdot 13$, ... because they have already been replaced
- And there are ways to implement it more elegantly, but the point is just to see how to program with lists.