

$$\sum_{k=1}^n p_i(1 - p_i) = \sum_{k=1}^n p_i - \sum_{k=1}^n p_i^2 = 1 - \sum_{k=1}^n p_i^2$$