

$$\pi_r(a) = U_r(x)$$