

$$\pi_r(\mathbf{X}) = \sum_{i=1}^r \alpha_i \mathbf{u}_i = \mathbf{U}_r \cdot (a_1, a_2, \dots, a_r)^t$$